

**BACHELOR OF TECHNOLOGY (CBCS - 2023)**  
**B. Tech. Sem-I Computer Science & Business Systems : WINTER: 2025**  
**SUBJECT: DISCRETE MATHEMATICS**

Day : Monday  
Date : 08/12/2025

W-27621-2025

Time : 10:00 AM-01:00 PM  
Max. Marks : 60

**N.B.**

- 1) All questions are **COMPULSORY**.
- 2) Figures to the **RIGHT** indicate **FULL** marks.
- 3) Draw neat diagrams **WHEREVER** necessary.
- 4) Use of non-programmable calculator is allowed

**Q.1** Explain Rules of inference for propositional logic: (with the help of suitable examples) (10)

- a) Modus Ponens                      b) Modus Tollens                      c) Hypothetical Syllogism  
d) Disjunctive Syllogism                      e) Resolution

**OR**

**Q.1** Let P & Q be the propositions:  
P : I bought a lottery ticket this week (10)

Q : I won the million dollar jackpot on Friday

Explain each of these propositions as an English sentence:

- a)  $\neg P$                       b)  $P \vee Q$                       c)  $P \rightarrow Q$                       d)  $P \wedge Q$   
e)  $P \leftrightarrow Q$                       f)  $\neg P \rightarrow \neg Q$                       g)  $\neg P \wedge \neg Q$                       f)  $\neg P \vee (P \wedge Q)$

**Q.2** What is canonical form? Explain CNF & DNF in detail with suitable examples. (10)

**OR**

**Q.2** What is multiset? Explain operations on multisets (union, intersection, difference and sum of multisets) with suitable examples. (10)

**Q.3** Explain various properties of relations with suitable examples. (10)

**OR**

**Q.3** Explain pigeonhole principle with suitable diagrams along with different cases. (10)

**Q.4** Explain 'semigroup' Algebraic structure, check whether the algebraic system (A, \*) whose table is given below, is a semigroup (10)

*	a	b	c
a	a	b	c
b	a	c	b
c	a	b	c

**OR**

**Q.4** Explain rings and group codes with suitable examples. Also explain Homomorphism, automorphism & Isomorphism of group. (10)

**Q.5** Solve the following recurrence relation with iteration method:  
 $T(P) = T(P-1) + 3$                        $P \geq 1$                       (10)  
&  $T(0) = 2$                       Also calculate the closed form for given equation.

**OR**

**Q.5** Explain permutation & combination function with suitable examples. Also calculate permutation for:- (10)  
How many necklace of 10 beads each can be made from 13 beads of different color?

**Q.6** Explain various types of graph along with suitable diagrams. (10)

**OR**

**Q.6** Explain Eulers path & Circuit and Hamiltonian path & circuit with suitable examples. (10)

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