

**BACHELOR OF TECHNOLOGY (CBCS) (2021-COURSE)**  
**Computer Science & Engineering**  
**B. Tech. Sem - II :SUMMER : 2023**  
**SUBJECT : MATHEMATICS FOR COMPUTING-II**

Day : Monday

Time : 10:00 AM-01:00 PM

Date : 22-05-2023

S-24024-2023

Max. Marks : 60

**N.B.:**

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.

**Q.1** Find the Fourier series of  $f(x) = x^2$  in  $(-\pi, \pi)$ . Hence show that (10)  

$$\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots = \frac{\pi^2}{6}$$

**OR**

**Q.1** Find the cosine series of  $\sin x$  in  $(0, \pi)$ . Hence show that (10)  

$$1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\pi}{4}$$

**Q.2** Find the Fourier sine and cosine transform of  $f(x) = e^{-x}$ . (10)

**OR**

**Q.2** If  $f_s(\lambda) = \frac{e^{-a\lambda}}{\lambda}$  then find  $f(x)$ . (10)

**Q.3** Obtain the Laplace transform of: i)  $t \sin^3 t$  ii)  $\frac{1 - \cos t}{t}$  (10)

**OR**

**Q.3** Find: i)  $L^{-1}\left(\frac{s}{s^2 + 4}\right)$  ii)  $L^{-1}\left(\frac{2s}{(s^2 - 4)^2}\right)$  (10)

**Q.4** Evaluate  $\iint_R x^{m-1} y^{n-1} dx dy$  where R is area bounded by  $x + y = k$ ,  $x = 0$ ,  $y = 0$ . (10)

**OR**

**Q.4** Change the order of following integration  $\int_0^1 \int_x^{1/x} f(x, y) dx dy$ . (10)

**Q.5** i) Find  $\nabla^2(e^r)$  where  $r = \sqrt{x^2 + y^2 + z^2}$  ii) Find  $\nabla \cdot (r^3 \bar{r})$ . (10)

**OR**

**Q.5** i) Find  $\nabla^2 f(r)$  where  $r = \sqrt{x^2 + y^2 + z^2}$  ii) Show that the vector field  
 $\bar{F} = (y^2 \cos x + z^2) \bar{i} + 2y \sin x \bar{j} + 2xz \bar{k}$  is conservative. (10)

**Q.6** Verify stoke's theorem for  $\bar{F} = x^2 \bar{i} + xy \bar{j}$  for the surface of a square lamina (10)  
 bounded by  $x = -1, x = 1, y = -1, y = 1$ .

**OR**

**Q.6** Find by using the Green theorem  $\int_C (xy - y^2) dx + x^2 y dy$  along the closed curve (10)  
 bounded by  $x = 1, y = 0$  and  $y = x$ .

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