

BACHELOR OF TECHNOLOGY (CBCS) (2021-COURSE)
B. Tech. Sem - II Computer Science & Engineering AI & ML : WINTER : 2024
SUBJECT: PROBABILITY & STATISTICS

Day : Saturday
Date : 07/12/2024

W-23930-2024

Time : 10:00 AM-01:00 PM
Max. Marks : 60

N.B :

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.
- 3) Draw neat and labeled diagrams **WHEREVER** necessary.
- 4) Use of non programmable **CALCULATOR** is allowed.
- 5) Assume suitable data if necessary.

- Q.1** A bag contains 5 white and 8 red balls. Two drawing of 3 balls are made such that (10)
- that
- i) the balls are replaced before the second trial and
 - ii) the balls are not replaced before the second trial. Find the probability that the first drawing will give 3 white and the second 3 red balls in each case.

OR

- Q.1** A company has two plants to manufacture cars. plant A manufacture 70 % of the cars and plant B manufacture 30%. At plant A, 80% if cars are rated standard quality and at plant B, 90% of cars are rated standard quality. A car is picked up to random and is found to be of standard quality. A car is picked up to random and is found to be of standard quality. What is the probability that it was come from plant B? (10)

- Q.2** A random variables X has the following probability distribution. (10)

| | | | | | | | | | |
|--------|---|----|----|----|----|-----|-----|-----|-----|
| X=x | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| P(X=x) | K | 3K | 5K | 7K | 9K | 11K | 13K | 15K | 17K |

- i) Determine the value of K.
- ii) Find $P(X < 3)$, $P(X \geq 3)$, $P(X < 5)$

OR

- Q.2** Let X be a continuous random variables with the following probability distribution : (10)

| | | | |
|---------|-----|-----|-----|
| X= x | -3 | 6 | 9 |
| P(X= x) | 1/6 | 1/2 | 1/3 |

Find $E(X)$ and $E(X^2)$ and using the laws of expectation, evaluate $E(2X+1)^2$.

- Q.3** X is normally distributed and the mean of X is 12 and S.D. is 4. Find out probabilities that (10)
- i) $X \geq 20$
 - ii) $X \leq 20$
 - iii) $0 \leq X \leq 12$
- (Given: $Z_{(0,2)} = 0.4772$, $Z_{(0,1)} = 0.3413$, $Z_{(0,3)} = 0.49865$)

OR

- Q.3** A manufacturer, who produces medicine bottles, finds that 0.1% of the bottles are defective. The bottle are packed in boxes containing 500 bottles. A drug manufacturer buys 100 boxes from the producer of bottles. Using Poisson distribution, find how many boxes will contain (10)
- i) No defective
 - ii) At least two defectives

P.T.O.

- Q.4 The marks obtained by 10 students in mathematics X and statistics Y are given below. Find the coefficient at correlation between X and Y (10)

| | | | | | | | | | | |
|---|----|----|----|----|----|----|----|----|----|----|
| X | 75 | 30 | 60 | 80 | 53 | 35 | 15 | 40 | 38 | 48 |
| Y | 85 | 45 | 54 | 91 | 58 | 63 | 35 | 43 | 45 | 44 |

OR

- Q.4 A sample of 12 fathers and their eldest sons gave the following data about their height in inches. Calculate coefficient of correlation between x and y. (10)

| | | | | | | | | | | | | |
|------------|----|----|----|----|----|----|----|----|----|----|----|----|
| Father (x) | 65 | 63 | 67 | 64 | 68 | 62 | 70 | 66 | 68 | 67 | 69 | 71 |
| Son (y) | 68 | 66 | 68 | 65 | 69 | 66 | 68 | 65 | 71 | 67 | 68 | 70 |

- Q.5 For 10 randomly selected observations the following data were recorded: (10)

| | | | | | | | | | | |
|---|---|---|---|----|---|----|----|----|----|----|
| X | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 6 | 7 |
| Y | 2 | 7 | 7 | 10 | 8 | 12 | 10 | 14 | 11 | 14 |

Determine the regression equation using non-linear form $Y = a + b_1x + b_2x^2$.

OR

- Q.5 Derive expression for regression lines on Y on X and X on Y. (10)

- Q.6 The following table gives the no. of refrigerators sold by 4 salesmen in three months May, June and July (10)

| Months | Salesmen | | | |
|--------|----------|----|----|----|
| | A | B | C | D |
| May | 50 | 40 | 48 | 39 |
| June | 46 | 48 | 50 | 45 |
| July | 39 | 44 | 40 | 39 |

- i) Is there a significant difference in the sales made by the four salesmen?
 ii) Is there a significant difference in the sales made during different months?

(Given: $F_{0.05}(3,6) = 4.76$, and $F_{0.05}(2,6) = 5.14$)

OR

- Q.6 If $r_{12} = 0.8963$, $r_{13} = 0.648$ and $r_{23} = 0.709$
 Find $r_{12.3}$ and $R_{1.32}$ (10)

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