

BACHELOR OF TECHNOLOGY (C.B.C.S.) (2021-COURSE)
 B. Tech. Sem - I Electrical & Computer Engineering : WINTER- 2022
 SUBJECT : PARTIAL DIFFERENTIATION & COMPLEX NUMBERS

Day : Monday
 Date : 9/1/2023

W-25143-2022

Time : 10:00 AM-01:00 PM
 Max. Marks : 60

N.B :

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.
- 3) Use of non-programmable **CALCULATOR** is allowed.
- 4) Draw neat and labeled diagram **WHEREVER** necessary.
- 5) Assume suitable data if necessary.

Q.1 Expand $(1+x)^{1/x}$ upto the term containing x^2 . [10]

OR

Q.1 Expand $e^{x \cos x}$ upto x^4 . [10]

Q.2 If $u = t^n e^{-r^2/4kt}$, then find the value of n for which $\frac{\partial u}{\partial t} = k \left(\frac{\partial^2 u}{\partial r^2} + \frac{2}{r} \frac{\partial u}{\partial r} \right)$, k is constant. [10]

OR

Q.2 If $u = \cos ec^{-1} \sqrt{\frac{x^{1/3} + y^{1/3}}{x+y}}$ find $x^2 u_{xx} + 2xy u_{xy} + y^2 u_{yy}$ [10]

Q.3 Find $\frac{\partial(u,v,w)}{\partial(x,y,z)}$ for $u^3 + v^3 + w^3 = x + y + z$ [10]
 $u^2 + v^2 + w^2 = x^3 + y^3 + z^3$
 $u + v + w = x^2 + y^2 + z^2$

OR

Q.3 Find the maximum and minimum values of $x^3 + 3xy^2 - 3x^2 - 3y^2 + 7$ [10]

Q.4 Verify divergence theorem for $\vec{F} = 2y^2 x \vec{i} + (xz^2 - y^3) \vec{j} + z^3 \vec{k}$ over the volume of a cube with edges of length unity parallel to the co-ordinate axes. [10]

OR

Q.4 Verify Green theorem for $\vec{F} = (xy + y^2) \vec{i} + x^2 \vec{j}$ C: $y = x$ and $y = x^2$ [10]

Q.5 Show that $u = \frac{1}{2} \log(x^2 + y^2)$ is harmonic and find its harmonic conjugate function. [10]

OR

Q.5 If $f(z)$ is an analytic function with constant modulus, show that $f(z)$ is constant. [10]

Q.6 Use residue theorem to evaluate $\int_0^{2\pi} \frac{\cos 3\theta}{5 - 4 \cos \theta} d\theta$ [10]

OR

Q.6 Solve $\oint_C f(z) dz$ where $f(z) = \frac{z^2}{(z-1)^2(z+2)}$ and $C: |z-2|=3$. [10]