

**BACHELOR OF TECHNOLOGY (CBCS) (2021-COURSE)**  
**B. Tech. Sem - II Computer Science & Engineering- AL & ML : WINTER : 2023**  
**SUBJECT : PROBABILITY & STATISTICS**

Day : Tuesday

Time : 10:00 AM-01:00 PM

Date : 21-11-2023

**W-23930-2023**

Max. Marks : 60

**N.B.:**

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.
- 3) Use of non-programmable **CALCULATOR** allowed.
- 4) Assume suitable data if necessary.

- Q.1** A can hit a target 3 times in 5 shots, B 2 times in 5 shots and C 3 times in 4 shots. They fire a volley. What is the probability that (10)
- i) two shots hit
  - ii) at least one shot hit?

**OR**

- Q.1** Machines  $M_1$ ,  $M_2$  and  $M_3$  manufacture identical items. Of their respective output 5%, 4% and 3% of items are faulty. On a certain day,  $M_1$  manufactured 25% of the total output,  $M_2$  has manufactured 30% and  $M_3$  the remainder. An item selected at random is found to be faulty. What is the probability that it was manufactured by the machine with the highest output? (10)

- Q.2** A continuous random variable  $X$  with p.d.f.  $f(x) = 3x^2$ ,  $0 \leq x \leq 1$  (10)
- 1) Verify that  $f(x)$  is p.d.f.
  - 2) Find  $a$  and  $b$  such that: i)  $P(x \leq a) = P(x > a)$  ii)  $P(x > b) = 0.05$

**OR**

- Q.2** A continuous random variable  $X$  with p.d.f.  $f(x) = Kx^2(1-x^3)$ , where  $K$  is a constant. Find the value of  $K$ , mean and variance. (10)

- Q.3** Let  $X$  is normal variate with mean 30 and S.D. 5. Find the probabilities that (10)
- i)  $26 \leq X \leq 40$
  - ii)  $X \geq 45$
  - iii)  $|X-30| > 5$
- (Given:  $A_{z=0.8}=0.2881$ ,  $A_{z=2}=0.4772$ ,  $A_{z=3}=0.4986$ ,  $A_{z=1}=0.3413$ )

**OR**

- Q.3** The following data due to Weldon shows the results of throwing 12 fair dice 4,096 times, a throw of 4, 5 or 6 being called success. (10)

Success	0	1	2	3	4	5	6	7	8	9	10	11	12
Frequency	-	7	60	198	430	731	948	847	536	257	71	11	-

Fit a binomial distribution and find the expected frequency.

**P.T.O.**

- Q.4 Calculate the coefficient of correlation between X and Y for the following: (10)

X	1	3	4	5	7	8	10
Y	2	6	8	10	14	16	20

OR

- Q.4 Find spearman's rank coefficient of correlation from the following data: (10)

X	50	66	34	21	15	79	42
Y	51	64	53	41	17	73	29

- Q.5 Obtain the equations of two lines of regression for the following data: (10)

X	1	2	3	4	5	6	7	8	9
Y	9	8	10	12	11	13	14	16	15

OR

- Q.5 Obtain the equations of two lines of regression for the following data. Also obtain the estimate value of X for Y=70. (10)

X	65	66	67	67	68	69	70	72
Y	67	68	65	68	72	72	69	71

- Q.6 In trivariate distribution  $\sigma_1 = 2, \sigma_2 = \sigma_3 = 3, r_{12} = 0.7, r_{23} = r_{31} = 0.5$ . Find (10)
- i)  $r_{23.1}$     ii)  $R_{1.23}$     iii)  $b_{12.3}, b_{13.2}$

OR

- Q.6 The following represents the study hours/day by four different students on 3 different days. (10)

Days	A	B	C	D
Monday	2	3	4	5
Tuesday	4	4	6	6
Wednesday	6	5	8	8

- a) Test whether the study hours of the different students are same?
- b) Test whether the study hours on different days are same?  
(Given:  $F_{0.05}(6,3) = 4.76, F_{0.05}(6,2) = 5.14$ )

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